



Advances in Earthquake Engineering

Stochastic Structural  
Dynamics in  
Earthquake Engineering

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WIT<sup>TM</sup>PRESS

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